An Image Fusion Algorithm Based on Wavelet Transform and Fourier Measurement Matrix

Yuli Yuan^{1,*}, Qiang Yang²

¹College of Computer Science, Neijian Normal University, China *Corresponding author:10273640@qq.com

²College of Computer and Information Engineering, Yibin University, China scyangqiang@163.com Received August 2017; revised August 2018

ABSTRACT. The traditional image fusion algorithms carry out fusion based on the information of all the pixels in the original images. This leads to the problem of high time and space complexity for the fusion algorithms. To solve this problem, this paper proposes an improved image fusion algorithm based on wavelet transform and Fourier random measurement matrix. The proposed fusion algorithm only acts on a small amount of data after the compressive sensing sampling. The image fusion is completed in the compressive sensing domain. The fused image is reconstructed by the orthogonal matching tracking algorithm. The experimental results show that this proposed image fusion algorithm based on wavelet transform and Fourier random measurement matrix has good performance. **Keywords:** Image Fusion, Wavelet Transform, Fourier Random Measurement Matrix, Orthogonal Matching Tracking Algorithm

1. Introduction. At present, there are three levels of image fusion: pixel-level fusion, feature-level fusion and decision-level fusion. The feature-level fusion first extracts the features of each original image. After the feature extractions on the texture, edge, corner, line and specific area of an image, the image fusion is completed with the extracted feature parameters. The decision-level fusion first extracts the features of original images. Then, the image fusion is completed according to the understandings of the extracted image features. The pixel-level fusion algorithm directly carries out the fusion process on image pixels. Therefore, the time complexity and space complexity are higher. The compressive sensing theory breaks through the requirements of traditional Nyquist sampling theorem, reduces the sampling data amount. This theory compresses the image data while acquiring the image. It provides new image acquisition and processing framework, and provides new research ideas for the image fusion with large data amount [1-4].

After the match of the to-be-fused images, the image fusion algorithm, which is based on compressive sensing theory, obtains the measured values of the two images by conducting dimensional reduction transform on the two images using the designed Fourier random measurement matrix. Then, the fusion of the measured values is carried out according to the fusion rule in the compressive sensing domain. Finally, the fused image is reconstructed according to the reconstruction algorithm of compressive sensing theory.

2. An Image Fusion Method Based On Wavelet Transform and Fourier Measurement Matrix.

2.1. The Measurement and Fusion of Image Dimensional Reduction. Firstly, the sparse representation of the original image is obtained with the wavelet transform. Then, the dimensional reduction measurement is carried out using Fourier random measurement matrix, and the image fusion is completed in the compressive sensing domain. The image fusion algorithm based on wavelet transform and Fourier random measurement matrix, and its implementation steps are shown as follows:

Step 1: Carry out accurate matching for two images F1 and F2.

Step 2: Carry out sparse transformation on image F1 and image F2 using wavelet transform. For an image F $(N \times N, N=2K)$:

$$F(x,y) = \begin{bmatrix} f_{0.0} & f_{0.1} & \dots & f_{0.2K-1} \\ f_{1.0} & f_{1.1} & \dots & f_{1.2K-1} \\ \dots & \dots & \dots & \dots \\ f_{2k-1.0} & f_{2K-1.1} & \dots & f_{2K-1.2K-1} \end{bmatrix}$$

The wavelet sparse transformation of an image is achieved with Mallat algorithm. It can be calculated with Equations from (1) to (4) $^{[5,12]}$.

$$LL_{x,y} = \frac{1}{4} \sum_{k_1,k_2=0}^{\iota} p_{k_1} p_{k_2} i_{k_1+2x,k_2+2y} = \frac{1}{4} (i_{2x,2y} + i_{2x,2y+1} + i_{2x+1,y} + i_{2x+1,2y+1})(1)$$

$$LH_{x,y} = \frac{1}{4} \sum_{q_1,k_2=0}^{l} p_{k_1} q_{k_2} i_{k_1+2x,k_2+2y} = \frac{1}{4} (i_{2x,2y} - i_{2x,2y+1} + i_{2x+1,y} - i_{2x+1,2y+1}) (2)$$

$$HL_{x,y} = \frac{1}{4} \sum_{k_1,k_2=0}^{l} q_{k_1} p_{k_2} i_{k_1+2x,k_2+2y} = \frac{1}{4} (i_{2x,2y} + i_{2x,2y+1} - i_{2x+1,y} - i_{2x+1,2y+1})(3)$$
$$HH_{x,y} = \frac{1}{4} \sum_{k_1,k_2=0}^{l} q_{k_1} q_{k_2} i_{k_1+2x,k_2+2y} = \frac{1}{4} (i_{2x,2y} - i_{2x,2y+1} - i_{2x+1,y} + i_{2x+1,2y+1})(4)$$

$$k_{1,k_2=0}$$

Step 3: Conduct dimensional reduction measurement on image F1 and image F2 with
Fourier random measurement matrix. The elements in the Fourier matrix are shown in
Equation (5) ^[6,12].

$$F_{j,k} = \frac{1}{\sqrt{N}} e^{i2\pi jk/N}(5)$$

Carry out dimensional reduction measurement on images, $X = \Phi F = \Phi \psi \mu = \Theta \mu$, and the measured values X_1, X_2 of the images are obtained.

Step 4: Carry out coefficients fusion on measured values X_1, X_2 .

To achieve better fusion performance, not only the fusion of the corresponding pixels on the original images should be considered during the image fusion, but also the local regions of the corresponding pixels should be taken into account. The variance Dev(X)and entropy E(X) of the local fusion region are used as the fusion parameters^[7]. The values of variance Dev(X) and entropy E(X)can be calculated according to Equations (6) and (7).

$$Dev(X) = \frac{1}{D_1 \times D_2} \sum_{0}^{D_1 - 1} \sum_{0}^{D_2 - 1} (G(X_{i,j}) - \overline{G}(X))^2 (6)$$

$$E(X) = -\sum_{i=0}^{L-1} P_i \log(P_i)(7)$$

In Equation (6), Dev(X) represents the variance (D1, D2 are small integers) of region $(D_1 \times D_2)X$. $G(X_{i,j})$ represents the measured value of (m, n) in the region X. $\overline{G}(X)$ represents the average value of the measured values for the region X. In Equation (7), E(X) represents the entropy, P_i represents the ratio of the pixels with gray value of i in the region X, and L is the gray scale. During the fusion of the measured values, the measured value of the central pixel of the region with lager variance Dev(X) and entropy E(X) is taken as the value of the fusion result.

2.2. Image reconstruction. In this paper, the orthogonally matching tracking algorithm (OMP) ^[8] is used for image reconstruction with the fused measurement values.

The implementation steps are as follows $^{[9,10,11]}$:

Step 1: ϕ represents the Fourier random measurement matrix, X denotes the observation vector, K is the sparse degree, r is the residual. The residual is initialized to $r^0 = X$, and the number of iterations is initialized to zero.

Step 2: Y_0 is used to represent the sparse solution of reconstruction, I denotes the index set, I = E.

Step 3: Calculate the correlation coefficient μ , $u = \phi^T r$, and calculate the maximum value of μ in the meantime. Then, add the corresponding index value of the maximum value in μ to the index set J.

Step 4: Add the corresponding elements of the index values in J to the set I. And set the corresponding elements in the Fourier random measurement matrix ϕ to 0.

Step 5: Solve the support set ϕ_I , $I = U \cup I$.

Step 6: Solve the approximate solution Y by using the least squares method, $Y = (\Phi_I^T \Phi_I)^{-1} \Phi_I X$.

Step 7: Calculate the residual $r = X - \Phi_I Y$.

Step 8: Judge the iteration termination condition. If |I| < 2K and also $nor(m) > \delta$, or $||r^n - r^{n-1}|| \le 10^{-6}$, then the number of iterations is incremented by 1, and then go to step 3 to continue, otherwise the iteration is terminated.

3. Evaluation Parameters for Image Fusion. Because image fusion is lack of standard image as reference image, the fusion result image cannot be compared with the reference image. Therefore, the traditional image processing performance evaluation parameters such as mean squared error (MSE), peak signal to noise ratio (PSNR) cannot be used for the objective evaluation of fusion experiment performance. This paper selected currently commonly used evaluation methods that do not need reference images to analyze the experimental results, which mainly includes spectral angle mapper (SAM) and improved SAM(ISAM).

The SAM is defined as follows^[13,14]:

$$SAM_UV = across \frac{\sum_i u_i v_i}{\sqrt{\sum_i u_i^2} \sqrt{\sum_i v_i^2}} (8)$$

The ISAM is defined as follows^[15]:

$$ISAM_{U}V = across\left(\frac{2\sum_{i}u_{i}v_{i}}{\sqrt{\sum_{i}u_{i}^{2}}\sqrt{\sum_{i}v_{i}^{2}}}\right)(9)$$

Where, and represent the vectors in the original images U and V, where, and represent the mean values of U and $V, U = \{u, u, ..., u\}V = \{v, v, ..., v\}, u \neq v$.

4. Experimental Analysis. In order to verify the effectiveness of the fusion algorithm, the image fusion method based on wavelet transform and Fourier measurement matrix, principal component analysis method, and pyramid method are used to carry out fusion experimental analysis on both full color image and visible light image. The fusion results are shown in Fig. 1.

Fig. 1 (a) is an infrared imaging image F1. Fig. 1 (b) is a visible light image F2, the image pixel size is 256 * 256. Fig. 1 (c) is the fusion result image based on principal component analysis. Fig. 1 (d) is the fusion result image based on pyramid method. Fig. 1(e) is the obtained fusion result image by the fusion algorithm based on wavelet transform and Fourier measurement matrix.



(a) Infrared image F1 (b) Image F2 from visible light imaging



(c) The fusion result image based on the principal component analysis(d) The fusion result image based on pyramid method



(e) The obtained fusion result image by the fusion algorithm based on wavelet transform and Fourier measurement matrix

Fig. 1 The fusion results for both infrared image and visible light image

The information entropy, average gradient, mutual information, SAM and ISAM are selected as the evaluation parameters to compare and analysis the experimental results. The 'I', 'V' and 'F' represent the infrared, visible light and fused images, respectively. The

evaluation parameters of the obtained fusion result image using three fusion algorithms are shown in Table 1.

Table 1	The e	valuation	parameters	of fusion	quality	for	\mathbf{both}	infrared	image	and	visible
light rem	ote sen	ising imag	e								

Eurien methed	Information Average		Mutual	CAM	TGAM	CAM	TGAM	Time
Fusion method	entropy	gradient	information	SAMIF	ISAMIF	SAMVF	ISAMVF	consumption(s)
Principal component analysis	6.923	0.023	1.867	0.2946	0.465	0.152	0.177	30
Pyramid method A Fusion Method	7.12	0.0341	1.835	0.257	0.349	0.208	0.212	94
Based on Wavelet								
Transform and	6 500	0.016	1.73	0.269	0.359	0.147	0.155	55
Fourier	0.526							
Measurement								
Matrix								
Pyramid method A Fusion Method Based on Wavelet Transform and Fourier Measurement _Matrix	7.12 6.528	0.0341	1.835 1.73	0.257	0.349	0.208	0.212	94 55

This paper carries out fusion experiments analysis on multi-spectral image and full color image. Fig. 2 (a) is a multi-spectral image, Fig. 2 (b) is a full-color image, and the image pixel size is 256 * 256. Remote sensing image fusion method based on wavelet transform and Fourier measurement matrix, principal component analysis method, and pyramid method are used to carry out fusion experimental analysis on both the full color image and multi-spectral image. The fusion results are shown in Fig. 2.

The 'M', 'P' and 'F' are used to represent multi-spectral, full color and fused images, respectively. The objective evaluation parameters of the three fusion algorithms are shown in Table 2.



(a) Multi-spectral image F1 (b) Full color image F2



(c) The fusion result image based on principal component analysis

(d) The fusion result image based on pyramid method



(e) The fusion result image of remote sensing image fusion method based on wavelet transform and Fourier measurement matrix

Fig. 2 The fusion results of full-color image and multi-spectral image

Table 2 The quality evaluation table of fused images for both multi-spectral and full-color remote sensing

Fusion method	Informat entropy	Average ion gradi- ent	e Mutual infor- mation	SAM_{M}	$_F$ ISAM $_M$	$_{F}SAM_{PI}$	$_{F}$ ISAM $_{PF}$	Time con- sumption(s)
Principal								
component	20.723	64.563	6.874	0.335	0.643	0.129	0.397	25
analysis Pyramid method A Fusion Method	19.212	74.521	7.117	0.155	0.560	0.193	0.386	90
Based on Wavelet								
Transform and Fourier	20.852	47.203	6.751	0.388	0.562	0.325	0.389	43
Measurement								
Matrix								

The experimental results show that the improved image fusion algorithm based on wavelet transform and Fourier measurement matrix achieved good evaluation parameters in multi-source image fusion experiments. In the fusion experiments of infrared imaging image with visible light image, and the fusion experiments of multi-spectral image with full-color image, the evaluation parameters of average gradient, mutual information, SAM and ISAM have achieved good experimental results. These experiments show that the improved image fusion algorithm based on wavelet transform and Fourier measurement matrix only acts on a small amount of measurement data after compressive sensing sampling, which greatly reduces the number of pixels involved in the fusion and decrease the time and space complexity of fusion. And the image fusion performance is better.

5. **Conclusions.** This paper applies compressive sensing theory to the image fusion process. An improved image fusion algorithm based on wavelet transform and Fourier measurement matrix is proposed. This proposed algorithm overcomes the problems of large data amount and high time complexity that exist in traditional image fusion algorithms. It only acts on a small amount of data after compressive sensing sampling. The image

fusion is completed in the compressive sensing domain. The fused data is reconstructed by the reconstruction algorithm of compressive sensing theory to obtain the fusion result image. This algorithm has achieved good experimental results.

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