## A New Provable Secure Certificateless Aggregate Signcryption Scheme

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ABSTRACT. These existed signcryption schemes have low aggregate signcryption efficiency. So in this paper, we propose a new certificateless aggregate signcryption scheme. The new method can reduce the computation number of bilinear pairings and improve the signcryption efficiency. It also can set any one from the users as an aggregator, and then the appointed aggregator will launch the signcryption protocol. Then the message is encrypted and aggregated. Finally, we give the security proof and make comparison to verify the effectiveness of our new scheme.

Keywords: Certificateless aggregate signcryption; Bilinear pairings.

1. Introduction. Signcryption [1,2] can guarantee confidentiality, integrity,

non-repudiation and authentication all signature and encryption function for message in a single logical step. It is more effective than traditional signature schemes. Malone-Lee[3] proposed a signcryption scheme based on identity, but this scheme dose not have semantic security[4]. Then many signcryption schemes were proposed[5-7].

In 2008, Selvi[8] proposed a signcryption scheme based on identity and gave the security proof. When number of signcryption was larger, ordinary signcryption had a low efficiency. Aggregation signcryption could aggregate several ciphertexts and provided batch verification, which greatly reduced the information transformation power consumption and the effectiveness of signcryption verification. So it was very suitable for the many-to-one mode in large-scale distributed communication. Ren[9] put forward a proven security signcryption scheme. In order to improve the efficiency of signcryption and shorten the length of ciphertext, Rao [10] proposed a new attribute-based signcryption (ABSC) scheme for LSSS-realizable access structures utilizing only 6 pairings and making the ciphertext size constant. Ch [11] proposed an efficient lightweight signcryption scheme based on HECC which fulfills all the security requirements. Cheng [12] proposed a corrected version of Liu et al's[13] scheme and proved his scheme was indistinguishable against adaptive chosen ciphertext attacks and was existentially unforgeable against chosen message attacks in the standard model. However, the above signcryption schemes use lots of bilinear pairings computation, the effective is very low. In order to improve the efficiency of certificateless aggregate signcryption, we present a new certificateless aggregate signcryption(NCAS) scheme based on Exclusive OR (XOR). NCAS improves computation efficiency by reducing the computation number of bilinear pairings. What's more, we give the formal security proof under random oracle model for NCAS scheme. The new scheme has indistinguishability against adaptive chosen cipher-text attacks and beingness and unforgeability of adaptive chosen message attacks. We also make an analysis for cipher-text length and computational cost.

The followings are the structures of this paper. There are preliminaries in section2. Section3 is security model. We detailed introduce the new certificateless aggregate sign-cryption scheme in section4. Section5 demonstrates the new scheme's performance and followed by a conclusion in section6.

2. **Preliminaries.** Assuming that  $G_1$  is a addition cyclic group of order q,  $G_2$  is a multiplication cyclic group of order q, where q is a  $\lambda$ -bit prime. p is a generator of  $G_1$ . And discrete logarithm problems in  $G_1$  and  $G_2$  are difficulty. e is a bilinear pairing  $e: G_1 \times G_2$  satisfying the following properties: bilinear, degenerative and computability.

- Computational Diffie-Hellman Assumption(CDHA): given (aP, bP) for unknown  $a, b \in_R Z_q^*$ , computing abP is difficulty.
- Computational Billinear Diffie-Hellman(CBDH): given (P, aP, bP, cP) for  $a, b, c \in_R Z_q^*$ , computing  $e(P, P)^{abc}$  is difficulty.

3. Security model. We first give two definitions for security model of certificateless aggregate signcryption (CAS): confidentiality and unforgeability. Table1 is the explanation for some parameters used in this paper.

$\operatorname{Symbol}$	Explanation
$\hbar$	challenger
$l_1, l_2$	adversary
$\sigma_i$	signcrypt value
$ID_i, ID_j$	identity
$ID_B$	user
$m_i$	plaintext
M	message
$P_0, P_{pub}$	system public key
$s \in Z_q^*$	main key
$U_i$	user
$\Delta$	state information
L	list
b	bit
$R_i$	key

TABLE 1. Parameters explanation

**Definition 1.** For a NCAS scheme, if there is no any polynomial orders of magnitude adversary  $l_1(l_1 \text{ can win with non-ignorable advantage in indistinguishability against adaptive chosen cipher-text attacks game), then the scheme has the security properties of indistinguishability against adaptive chosen cipher-text attacks[13-15].$ 

1. System initialization. Challenger  $\hbar$  generates a system public parameter and sends it to adversary  $l_1$ , and saves the system main key.

Stage 1. Adversary can adaptively make the following polynomial orders of magnitude query.

- (a) Secret value query.  $l_1$  inputs  $(ID_i, R_{1,i})$  to make query and gets secret value  $(s_{1,i}, s_{2,i})$ .
- (b) Signeryption query.  $l_1$  inputs  $(ID_i, ID_B, m_i)$  to make query and gets signeryption  $\sigma_i = (v_i, c_i, R_i) = Signerypt(ID_i, ID_B, m_i).$
- (c) De-signcrypt query.  $l_1$  inputs signcryption  $\sigma_i$  and identity  $(ID_i, ID_j)$  to make query.  $\hbar$  can make de-signcrypt and sends the  $(\sigma_i, ID_i, ID_j)$  to  $\hbar$ .

Stage 2. Similarly to stage 1,  $\hbar$  can adaptively make the polynomial orders of magnitude query. And  $\hbar$  cannot query the private key of  $ID_B$  or make de-signcrypt query.

Guess stage. At last,  $\hbar$  submits a bit b'. If b' = b, then  $\hbar$  wins this game. The advantage of adversary in this game is:

$$adv(\hbar) = |Pr[b' - b] - 0.5|.$$
 (1)

**Definition 2.** For a NCAS scheme, if there is no any polynomial orders of magnitude adversary  $l_1(l_1 \text{ can win with non-ignorable advantage in adaptive chosen message attacks game), then the scheme has the beingness and unforgeability properties of adaptive chosen message attacks.$ 

- System initialization. Challenger  $\hbar$  generates a system public parameter  $\Omega$  and sends it to adversary  $l_2$ , and saves the system main key.
- Query stage. Adversary  $l_2$  executes the query similar to definition 1.
- Guess stage. Adversary  $l_2$  generates a triple  $(\sigma_i, ID_i, ID_B)$ , where secret value of  $ID_B$  has not been queried.  $\sigma_i$  is not the result by query. So if the result of  $unsigncrypt(\sigma_i, ID_i, ID_B)$  is False, then adversary  $l_2$  will win this game.

# 4. New certificateless aggregate signcryption. Detailed processes of NCAS are as follows.

- Step 1. System initialization. Supposing security parameter k, prime  $q \ge 2^k$ .  $(G_1, +)$  and  $(G_2, +)$  are cyclic groups of order q. Bilinear mapping  $e : G_1 \times G_1 \to G_2$ ;  $H_1 : 0, 1^* \times G_1 \to G_1$ ;  $H_2, H_3 : 0, 1^* \times G_1 \to Z_q^*$ ;  $H_4 : G_1 \times 0, 1^* \to G_1$  are four impact resistance hash functions. P is a generator of  $G_1$ . KGC randomly selects  $s \in Z_q^*$  as system main key. Setting system public key  $P_0 = sP$ , message space  $M = 0, 1^*$ . System public parameter  $\Omega = G_1, G_2, e, q, P, P_0, H_1, H_2, H_3, H_4$ .
- Step 2. Generate user key. User  $U_i$  selects random number  $s_{1,i} \in Z_q^*$  as a secret value. Then it computes public key  $R_{1,i} = s_{1,i}P$ .
- Step 3. Extract part private key of user. User  $U_i$  sends message to KGC. KGC first calculates  $R_{2,i} = H_1(ID_1, R_{1,i})$ , then calculates part private key  $s_{2,i} = sR_{2,i}$ .  $s_{2,i}$  will be sent to corresponding user  $U_i$  trough secure channel. So the signature private key and public key of user are  $(s_{1,i}, s_{2,i})$  and  $(R_{1,i}, R_{2,i})$  respectively.
- Step 4. Individual signeryption. Aggregation signers select the entity  $U_0$ , its identity is  $ID_0$ . User  $U_i$  makes signeryption for message  $m_i$ , then sends it to user  $ID_B$ . The process is as follows:
  - $-U_0$  randomly selects  $u_0 \in Z_q^*$  and calculates  $R_0 = u_0 P$ , then outputs  $R_0$ .
  - After  $U_i$  receives  $R_0$ , it randomly selects  $r_i \in \mathbb{Z}_q^*$ .
    - 1. Compute  $R_i = r_i P$ .
    - 2. Compute  $a_i = e(r_i P_{public}, R_{2,B})$ .
    - 3. Compute  $c_i = H_2(\alpha_i, ID_B) \oplus (ID_i||m_i)$ . (In this paper, we stipulate that both sides of XOR have the same length.)

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- 4. Compute  $h_{i1} = H_3(ID_i||m_i, ID_B)$  and  $h_{i2} = H_4(R_0, \Delta)$ . Where  $\Delta \in 0, 1^*$  is status messages.
- 5. Compute  $v_i = s_{2,i}h_{i1} + (r_i + s_{1,i})h_{i2}$ . So  $U_i$  sends the signcryption  $\sigma_i = (v_i, c_i, R_i)$  of message  $m_i$  to  $ID_B$ .
- Step 5. Aggregation signeryption. Aggregation signer  $U_0$  receives n signeryption  $\sigma_i = (v_i, c_i, R_i) (i = 1, 2, \dots, n)$ . Compute  $v = \sum_{i=1}^n v_i$ , therefore, aggregation signeryption is  $\sigma = \langle c_i, R_{i=1}^n, V \rangle$ .
- Step 6. De-signcryption.  $ID_B$  executes de-signcryption.
  - Calculate  $\alpha_i = e(R_i, s_{2,B}) = e(r_i P_{public}, R_{2,B}).$
  - Calculate  $ID_i || m_i = H_2(\alpha_i, ID_B) \oplus c_i$ .
  - Calculate  $h_{i1} = H_3(ID_i||m_i, ID_B)$  and  $h_{i2} = H_4(R_0, \Delta)$ . If  $e(V, P) = e(\sum_{i=1}^n h_{i1}R_{2,i}, P_0)e(h_{i2}\sum_{i=1}^n (R_i + R_{1,i}))$  is true, then it outputs
  - message  $ID_i || m_i$ . Otherwise, the signcryption is invalid.

### 5. Security and performance analysis.

#### 5.1. Security analysis.

**Theorem 5.1.** Correctness of the NCAS scheme.

$$e(V,P) = e(\sum_{i=1}^{n} (s_{2,i}h_{i1} + (r_i + s_{1,i})h_{i2}), P)$$
(2)

$$= e(\sum_{i=1}^{n} s_{2,i} h_{i1}, P) e(\sum_{i=1}^{n} ((r_i + s_{1,i}) h_{i2}), P)$$
(3)

$$= e(\sum_{i=1}^{n} h_{i1} R_{2,i}, P_0) e(h_{i2}, \sum_{i=1}^{n} (R_i + R_{1,i})).$$
(4)

**Theorem 5.2.** Based on CDHA and CBDH assumption, NCAS scheme satisfies IND-CCA2 security.

**Proof.** l owns (P, aP, bP, cP). Adversary  $\hbar$  makes a following interaction with l. System initialization. l sets  $P_0 = aP$  and selects system parameter  $G_1, G_2, e, q, P, P_{0}, H_1, H_2, H_3, H_4$ , then sends it to  $\hbar$ .

- Stage 1. Query.  $\hbar$  executes the following query.
  - 1.  $H_1$  query. l maintains list  $L_1 = (ID_i, R_{1,i}, R_{2,i}, x_i, c_i)$ .  $L_1$  is initiated to be 0. When  $\hbar$  inputs  $ID_i, R_{1,i}, l$  does the following response.
    - If the corresponding query of  $(ID_i, R_{1,i})$  has been in the list  $L_1$ , then it outputs  $R_{2,i}$ .
    - Otherwise, l randomly selects  $c_i \in 0, 1$ . Supposing the probability of getting  $c_i = 0$  is  $\delta$ , then the probability of getting  $c_i = 1$  is  $1 \delta$ . Randomly select  $x_i \in Z_q^*$ , if  $c_i = 0$ , l returns  $R_{2,i} = x_i b P$ . If  $c_i = 1$ , l returns  $R_{2,i} = x_i P$ . At last,  $(ID_i, R_{1,i}, R_{2,i}, x_i, c_i)$  is put into  $L_1$ .
  - 2.  $H_2$  query. l maintains list  $L_2 = (\alpha_i, ID_B, h_i)$ .  $L_2$  is initiated to be 0. When  $\hbar$  inputs  $(\alpha_i, ID_B)$ , l does the following response.
    - If the corresponding query of  $(\alpha_i, ID_B)$  has been in the list  $L_2$ , then it outputs  $\gamma_i$ .
    - Otherwise, l randomly selects  $h_i \in_R Z_g^*(i \neq 0)$ . Output  $h_i$ . At last,  $\alpha_i, ID_B, h_i$  is put into  $L_2$ .
  - 3.  $H_3$  query. l maintains list  $L_3 = (ID_i, m_i, ID_B, h_{i1})$ .  $L_3$  is initiated to be 0. When  $\hbar$  inputs  $(ID_i, m_i, ID_B)$ , l does the following response.
    - If the corresponding query has been in the list  $L_3$ , then it outputs F.
    - Otherwise, l randomly selects  $h_{i1} \in_R Z_g^*(i \neq 0)$ . Output  $h_{i1}$ . At last,  $(ID_i, m_i, ID_B, h_{i1})$  is put into  $L_3$ .
  - 4.  $H_4$  query. l maintains list  $L_4 = (R_0, \Delta, \mu_i, h_{i2})$ .  $L_4$  is initiated to be 0. When  $\hbar$  inputs  $(R_0, \Delta)$ , l does the following response.

- If the corresponding query of  $R_0, \Delta$  has been in the list  $L_4$ , then it outputs  $h_{i2}$ .
- Otherwise, *l* randomly selects  $(\mu_i \in_R Z_g^*(i \neq 0))$ . Compute  $h_{i2} = \mu_i P$ . Output  $h_{i2}$ . At last,  $(R_0, \Delta, \mu_i, h_{i2})$  is put into  $L_4$ .
- 5. Secrete value query. l maintains list  $L_K = (ID_i, R_{1,i}, R_{i2}, s_{1,i}, s_2, i)$ .  $L_K$  is initiated to be 0. When  $\hbar$  inputs  $(ID_i, R_{1,i})$ , l does the following response.
  - If the corresponding query has been in the list  $L_K$ , then it outputs  $(s_{1,i}, s_{2,i})$ . If  $R_{1,i}$  is replaced, then it outputs F.
  - Otherwise, l randomly selects  $s_{1,i} \in_R Z_g^*$  and outputs  $(s_{1,i}, s_{2,i} = sR_{2,i})$ . At last, it puts  $(ID_i, R_{1,i}, R_{i2}, s_{1,i}, s_{2,i})$  into  $L_K$ .
- 6. Public key query. l inputs  $ID_i$  to make query and does the following response. - If  $ID_i$  has been in the list  $L_K$ , then it outputs  $R_{1,i}$ .
  - Otherwise, if  $s_{1,i}$  is true, then compute  $R_{1,i} = s_{1,i}P$ . Otherwise, l randomly selects  $s_{1,i} \in_R Z_g^*$  and outputs  $(R_{1,i} = s_{1,i}P)$ . At last, it puts  $ID_i, R_{1,i}, s_{1,i}$  into  $L_K$ .
- 7. Public key replacement query. l inputs  $(ID_i, R_{1,i}^*)$  to make public key replacement query and does the following response.
  - If  $ID_i$  has been in the list  $L_K$ , then  $R_{1,i}^*$  replaces  $R_{1,i}$ . And  $s_{1,i} = F$ .
  - Otherwise, the new  $(ID_i, ID_B, m_i)$  will be added into  $L_K$ .
- 8. Signcryption query. l inputs  $(ID_i, ID_B, m_i)$  to make query.  $\hbar$  does the following response after asking  $L_1$ .
  - If  $c_i = 1$ , it uses the original signcryption algorithm to encrypt message and outputs the result.
  - If  $c_i = 0$ , l cancels the query.
- 9. De-signcryption query. l inputs aggregation signcryption  $\sigma$  to make query. The receiver of signcryption is  $ID_B$ .  $\hbar$  checks that whether  $L_1$  is in the corresponding data  $(ID_i, R_{1,i}, R_{2,i}, s_{2,i}, x_i, c_i)$  of signcryption users'  $ID_i$ . If  $L_1$  is not in that, then l cancels the query. Otherwise, l uses the general de-signcryption algorithm to decrypt message.

In the simulation process, l may generate two same length messages  $m_{i0}$  and  $m_{i1}$ . It randomly selects parameters and runs the signcryption algorithm to get signcryption and aggregation signcryption  $\sigma_i, U_i$  of message  $m_{ib}$ . Then it returns  $\sigma^*$  to adversary  $\hbar$ .

• Stage 2 is similar to stage 1. However, adversary  $\hbar$  cannot make de-signcryption query for  $\sigma^* = \langle c_i, R_{i_{i=1}}^n, R, V \rangle$  and also cannot make  $H_1$  query and secret value query for  $ID_B$ .

Finally,  $\hbar$  returns Guess. If equation is true, then output 1. Otherwise, output 0. Because adversary  $\hbar$  cannot make de-signcryption query for  $\sigma^* = \langle c_i, R_{i=1}^n, R, V \rangle$ , so it needs to use  $(\alpha_i, ID_B)$  to make  $H_2$  query.  $\alpha_i = e(R_i, s_{2,B})$ .  $s_{2,B}$  is the private key of receiver. And  $s_{2,B} = abP$ . Set  $R_1 = cP$ . We can get:  $\alpha_i = e(R_i, s_{2,B}) = e(cP, abP) = e(P, P)^{abc}$ .

**Theorem 5.3.** Under the random oracle model, if the discrete logarithm problem(DLP) is difficulty, then our new aggregation signcryption scheme is security for any polynomial time adversary  $\hbar$ .

**Proof.** *l* has a DLP instance  $(P, Q = s_{1,r})P$ . The aim of *l* is to compute  $s_{1,r}$ . Assuming that a adversary  $\hbar_2$  satisfies polynomial time condition. Its proof is similar to proof of theorem 1. The following is the different part.

Private key query.  $\hbar_2$  inputs  $(ID_i, R_{1,i})$  to make query. l does the following response. If the corresponding  $R_{1,i}$  in  $L_1$  has been replaced, then return F. Otherwise,  $ID_i = ID_r$ ,  $l \text{ recovers } (ID_i, R_{1,i}, R_{2,i}, s_{1,i}, s_{2,i}) \text{ in list } L_1 \text{ and returns } (ID_i, R_{1,i}, R_{2,i}, *, *).$  Otherwise,  $ID_i \neq ID_r, l \text{ recovers } (ID_i, R_{1,i}, R_{2,i}, s_{1,i}, s_{2,i}) \text{ in list } L_K \text{ and returns } (R_{1,i}, R_{2,i}, s_{1,i}, s_{2,i}).$ 

Finally,  $\hbar_2$  returns a fake information which is contained in a ciphertext sent by  $ID_r$  to receiver  $ID_B$ . l uses decryption oracle machine to decrypt message, which can lead to disclose forger  $(ID_i, m_i, v_i)$ . If l makes right guess, namely  $ID_i = ID_r$  and  $ID_B \neq ID_r$ , then decryption is finished. If  $\sigma = \langle c_i, R_{ii=1}^n, V \rangle$  is an effective aggregation signeryption including  $(c_r, m_r, R_r, v_r)$ , and  $\sigma$  will be sent to  $ID_B$ . Then new algorithm can use oracle to obtain two legal signeryption information  $(ID_r, m_r, v'_r)$  and  $(ID_r, m_r, v''_r)$ , they meet  $V'_r = s_{2,r}h'_{r1} + (r_r + s_{1,r})h'_{r2}$  and  $V''_r = s_{2,r}h''_{r1} + (r_r + s_{1,r})h''_{r2}$ . Where  $h'_{r1} \neq h''_{r1}$ ,  $h'_{r2} \neq h''_{r2}$ . l can calculate  $s_{1,r}$  successfully. Therefore, our new scheme has existential unforgeability against adaptive chosen messages attacks.

5.2. **Performance analysis.** We make a comparison to FAAS[17], PSIAS[18], MM-CAS[19] and PSCHS[20] with our NCAS method. The explanation of symbols in this section: p: bilinear operation. e: exponent operation. s: point multiplication operation in  $G_1$ .  $|G_1|$ : the element length of corresponding group. |m|: the length of message. |U|: the length of user identity. |DEMK|: the KEY length of DEM[21].

Table 2 shows the calculation about the five algorithms. And we can know that signcrypter with NCAS only needs one pairing operation and two point multiplication operations in signcryption stage less than FAAS, PSIAS, MMCAS and PSCHS. In designcryption stage, NCAS needs n + 3 pairing operations obviously superior to PSCHS. The pairing operation number is more than FAAS, PSIAS and MMCAS. In that our new scheme dose not need exponent operation, the total calculation is superior to FAAS, PSIAS and MMCAS when n is big.

Scheme	Signcryption	De-Signcryption
FAAS	3ne	(n+1)p+(3n-3)s
PSIAS	n(p+e)+2s	3ns+np
MMCAS	3ne+np+ns	np+ns
PSCHS	2n(e+p)	6np+ne
NCAS	n(p+2s)	(n+3)p

TABLE 2. Calculation comparison with different schemes

In order to specifically analyze running time, we use the A type elliptic curve to test in jpbc database. Setting message m = 512 bit,  $|G_1| = |G_2| = |G_{k-1}| = 160$  bit,  $|Z_q^*|$ bit. n = 5. Then we record the running time with the above schemes as table3 from MATLAB platform. Its unit is second.

TABLE 3. Calculation time comparison with different schemes

Scheme	Signcryption time	De-Signcryption time
FAAS	513.348194	531.508835
PSIAS	614.040094	579.664869
MMCAS	819.531384	306.183189
PSCHS	681.116829	1187.770164
NCAS	442.922349	271.107759

Table 3 shows that the running time with NCAS is less than other schemes. It is the optimal scheme.

Next, we compare the ciphertext length as table4. PSCHS only has the non-signcryption length. From the table, the obvious is that although FAAS has the shortest ciphertext

length, it does not has the certificateless characteristic. When message space length is less than  $|G_{k-1}| = |G_2|$ , NCAS is the best choice.

Scheme	Length of Signcryption	Length of De-Signcryption
FAAS	$m( U  +  G_1 )$	$\frac{1}{ U  +  G_1 }$
PSIAS	$m( U  +  m  + 3 G_1  + Z_q^*)$	$m( U  +  m  + 2 G_1  + Z_q^*) +  G_1 $
MMCAS	$m( U  +  G_2  +  G_1  +  G_{k-1} )$	$m( U  +  G_2  +  G_1 ) +  G_{k-1} $
PSCHS	$m( U  +  G_2  + 2 G_1  + DEMK )$	
NCAS	$m( U  +  m  + 2 G_1 )$	$m( U  +  m  +  G_1 ) +  G_1 $

TABLE 4. Calculation comparison with different schemes

6. **Conclusions.** This paper proposes a new certificateless aggregate signcryption scheme. The new scheme can specify any user as aggregators. And aggregators can make initiation protocol. It has the characteristic of certificateless cryptosystem by using bilinear pairings to realize the aggregation for signcryption. Under the random oracle model, we proof the unforgeability of new scheme based on cryptology difficult problem. Finally, we make comparison to computational cost and ciphertext length. Results show that the new scheme not only increase ciphertext length, it also improves the calculation efficiency of certificateless aggregate signcryption.

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